

The Parabola

When Sun light (parallel rays) falls onto a correctly aligned parabolic mirror it will be reflected back towards a single point known as the focus. The parabolic mirror therefore directs the energy arriving over its surface to a 'hot spot' at the focus. You can use this energy to heat something.

The basic shape of a parabola is derived from the equation:

$$y^2 = 4ax \quad [1]$$

Where y represents the distance away from the mirror centre and x represents the 'height above' the centre, see figure 1 and 2. The constant a is known as the focal length - the distance from the origin to the focus point.

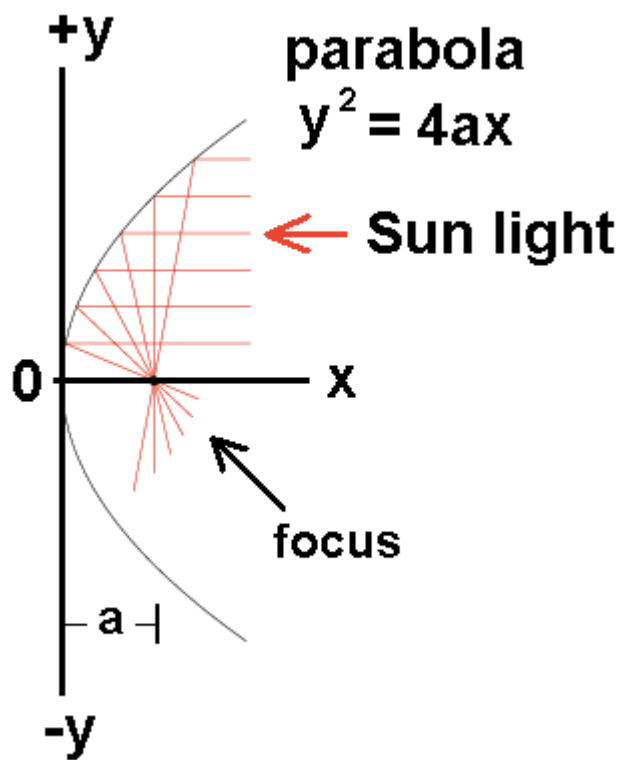


Figure 1. The basic geometry of a parabola mirror. Light rays coming from infinity will tend to be reflected towards a point called the focus.

If we want to make a parabolic reflector to our own particular specification i.e. in terms of its size D (i.e. having maximum $y = D/2$), height h and focal length a , then equation 1 becomes:

$$a = D^2/16h \quad [2]$$

A simple curved plane (rather than dish shape) solar heater is shown in photo 1 and we shall use this as an example, of course what follows can also be used for a full 'dish shaped' parabola and for much larger designs.

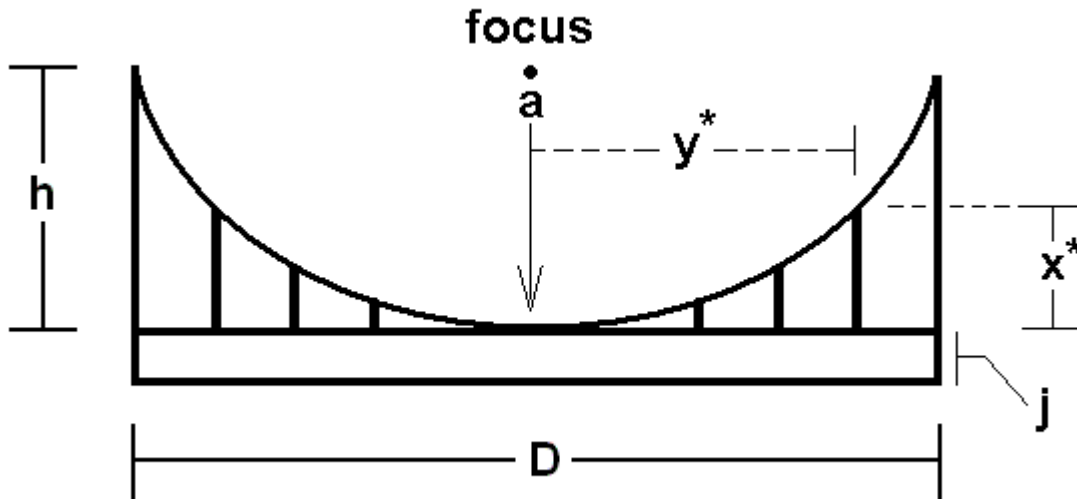


Figure 2. Parabolic surface made using i) a cut-out template or ii) by thin sheet fixed to vertical wooden supports. The position (y^*) and height (x^*) of each support (point) is calculated from the equation 1 and 3. A set of x and y values for the model in photo 1 is give in table 1. D -length, h -height, a -focus and j (an offset used to make the template version, see text).

To make it easy to locate the focal point when we are using it, I chose to design the mirror surface height (h) to be the same value as a - the focus distance above the center of the mirror (so $a = h$ in this example 11 cm). In this case finding the focus is simple - imagine a line going across the top of the device, the centre of this line is where the focus is.

Rearranging equation 2 we get the diameter / length of the solar heater D to be:

$$D^2 = 16ah, \text{ so using } h = a = 11 \text{ cm we get:}$$

$$D = \sqrt{(16 \times 11 \times 11)} = \sqrt{(1936)} = 44 \text{ cm}$$

We have $y^2 = 4ax$ and $a = 11 \text{ cm}$

For the solar heater shown in photo 1 we get $x = y^2/44$

[3] (all dimensions in cm)

Now that we have chosen the basic quantities for the parabola we can compute the x and y coordinates from equation 1 and 3. Some of these are tabulated in table 1. To re-cap, the y axis represents the distance away from the mirrors centre while x represents the 'height' above the base, the lowest point of the mirror (its centre).

You can also make a parabola support by cutting two side (parabola shaped) templates, see photo 1. In this case when marking up simply add a few cm (j in figure 2) to all the x values otherwise the template will diminish to zero thickness at the centre and it will all fall apart!

Table 1 - y and x values derived from equation 3 for the parabolic solar heater shown in photo 1.

$\pm y$ (cm)	y^2	$y^2/44$	x (cm)
0	0	0	0
1	1	1/44	0
2	4	4/44	0.1
3	9	9/44	0.2
4	16	16/44	0.3
5	25	25/44	0.6
6	36	36/44	0.8
7	42	42/44	0.9
8	64	64/44	1.5
...
20	400	400/44	9.1

and so on for larger values of y